



Math Review (<http://goo.gl/rTQmcL>)
Essential Academic Skill Enhancement (EASE) workshop series



This workshop reviews the basics of algebra through pre-calculus to help prepare you for college calculus.

We will discuss:

- Rational Equations
- Radical Equations
- Simple Exponents
- Not-So-Simple Exponents



- Quadratic Equations
- Trigonometry
- Composite Functions

Assessment Set 1:

1. Rational Equations: $\frac{3}{x+2} - \frac{1}{x} = \frac{1}{5x}$ (hint: make the common denominator of $5x(x+2)$).

- $\left(\frac{3}{x+2}\right)\left(\frac{5x}{5x}\right) - \left(\frac{1}{x}\right)\left(\frac{5(x+2)}{5(x+2)}\right) = \left(\frac{1}{5x}\right)\left(\frac{x+2}{x+2}\right)$
- $\left(\frac{15x}{5x(x+2)}\right) - \left(\frac{5x+10}{5x(x+2)}\right) = \frac{x+2}{5x(x+2)}$
- $15x - (5x + 10) = x + 2$
- $10x - 10 = x + 2$
- $9x = 12$
- $\underline{x = \frac{12}{9} = \frac{4}{3}}$

2. Radical Equations: $\sqrt{9x^2 + 4} = 3x + 2$

- $(\sqrt{9x^2 + 4})^2 = (3x + 2)^2$
- $9x^2 + 4 = (3x + 2)(3x + 2)$
- $9x^2 + 4 = 9x^2 + 12 + 4$
- $0 = 12x$
- $\underline{0 = x}$

3. Simple Exponents: $3^{2x-1} = 27$ (hint: What can you do to 27 to make it have base 3?)

- $3^{2x-1} = 27$
- $3^{2x-1} = 3^3$
- $2x - 1 = 3$
- $2x = 4$
- $\underline{x = 2}$

4. Not-So-Simple Exponents: $3(2^{x+4}) = 350$ (hint 1: Isolate the variable first; hint 2: Use natural log because of calculator function)

- $2^{x+4} = \frac{350}{3}$
(Note: $350/3$ is not solved out because of rounding, it is best to keep it in fraction form until plugging in to the calculator)
- $\ln(2^{x+4}) = \ln\left(\frac{350}{3}\right)$
- $(x + 4) \ln(2) = \ln\left(\frac{350}{3}\right)$
- $x + 4 = \frac{\ln\left(\frac{350}{3}\right)}{\ln(2)}$
- $\underline{x = \frac{\ln\left(\frac{350}{3}\right)}{\ln(2)} - 4 = \underline{\underline{2.866}}}$

5. Quadratic Equations: $2x^2 - 4x - 3 = 0$; Round answer to 2 decimal places.

$$\begin{aligned} \text{➤ } x &= \frac{-(-4) \pm \sqrt{(-4)^2 - 4(2)(-3)}}{2(2)} \\ \text{➤ } x &= \frac{4 \pm \sqrt{16+24}}{4} = \frac{4 \pm \sqrt{40}}{4} = \frac{4 \pm \sqrt{4}\sqrt{10}}{4} \\ \text{➤ } x &= \frac{4 \pm 2\sqrt{10}}{4} = \frac{2(2 \pm \sqrt{10})}{2(2)} = \frac{2 \pm \sqrt{10}}{2} \\ \text{➤ } x &= \frac{2 - \sqrt{10}}{2} \text{ AND } x = \frac{2 + \sqrt{10}}{2} \\ \text{➤ } x &\approx \underline{\underline{-0.58}} \text{ AND } x \approx \underline{\underline{2.58}} \end{aligned}$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

6. Trigonometry: $\cos^2(x) + \cos(x) = \sin^2(x)$ (hint: Use the trigonometric identity to have only 1 trig function: $\sin^2(t) + \cos^2(t) = 1$)

$$\begin{aligned} \text{➤ } \cos^2(x) + \cos(x) &= \sin^2(x) \\ \text{➤ } \cos^2(x) + \cos(x) &= 1 - \cos^2(x) \\ \text{➤ } 2\cos^2(x) + \cos(x) - 1 &= 0 \\ \text{➤ } (2\cos(x) - 1)(\cos(x) + 1) &= 0 \\ \text{➤ } \underline{\underline{\cos(x) = 1/2}} \text{ AND } \underline{\underline{\cos(x) = -1}} \end{aligned}$$

7. Composite Functions: $f(x) = 2x + 3$ and $g(x) = -x^2 + 5$; find $f(g(1))$

$$\begin{aligned} \text{➤ } &= f(-x^2 + 5) \quad \dots \text{ setting up to insert the original input} \\ \text{➤ } &= f(-1^2 + 5) \\ \text{➤ } &= f(-1 + 5) \\ \text{➤ } &= f(4) \\ \text{➤ } &= 2x + 3 \quad \dots \text{ setting up to insert the new input} \\ \text{➤ } &= 2(4) + 3 \\ \text{➤ } &= 8 + 3 \\ \text{➤ } &= \underline{\underline{11}} \end{aligned}$$

Assessment Set 2:

8. Rational Equations: $\frac{n-4}{n+4} = \frac{1}{n-5} + 1$

- $((n+4)(n-5))\left(\frac{n-4}{n+4}\right) = \left(\frac{1}{n-5} + 1\right)((n+4)(n-5))$
- $(n-5)(n-4) = n+4 + (n+4)(n-5)$
- $n^2 - 9n + 20 = n^2 - 16$
- $-9n + 20 = -16$
- $-9n = -16 - 20$
- $-9n = -36$
- $n = \frac{-36}{-9}$
- $n = \frac{36}{9}$
- **$n = 4$**

9. Radical Equations: $\sqrt{k-9} - \sqrt{k} = -1$

- Option 1 (the better option)
 - $(\sqrt{k-9} - \sqrt{k})(\sqrt{k-9} + \sqrt{k}) = (-1)(\sqrt{k-9} + \sqrt{k})$
 - $k - 9 - k = -\sqrt{k-9} - \sqrt{k}$
 - $\sqrt{k-9} + \sqrt{k} = 9$
 - $\left\{ \begin{array}{l} \sqrt{k-9} - \sqrt{k} = -1 \\ \sqrt{k-9} + \sqrt{k} = 9 \end{array} \right\}$
 - $2\sqrt{k-9} = 8$
 - $\sqrt{k-9} = 4$
 - $k - 9 = 16$
 - $k = 25$
- Option 2 (the not as good option)
 - $(\sqrt{k-9} - \sqrt{k})^2 = (-1)^2$
 - $-2\sqrt{k}\sqrt{k-9} + (\sqrt{k})^2 + (\sqrt{k-9})^2 = 1$
 - $2k - 2\sqrt{k}\sqrt{k-9} - 9 = 1$; $-2k$ from both sides
 - $-2\sqrt{k}\sqrt{k-9} - 9 = 1 - 2k$; $+9$ to both sides
 - $-2\sqrt{k}\sqrt{k-9} = 10 - 2k$
 - $\frac{-2\sqrt{k}\sqrt{k-9}}{-1} = \frac{10-2k}{-1}$
 - $2\sqrt{k}\sqrt{k-9} = 2k - 10$
 - $(2\sqrt{k}\sqrt{k-9})^2 = (2k - 10)^2$
 - $4(k-9)k = 4k^2 - 40k + 100$
 - $4k^2 - 36k = 4k^2 - 40k + 100$; $-(4k^2 - 40k + 100)$ from both sides
 - $4k - 100 = 0$
 - $4k = 100$
 - **$k = 25$**

10. Simple Exponents: $3^{1-2x} = 243$

- $3^{1-2x} = 3^5$
- $1 - 2x = 5$
- $-2x = 5 - 1$
- $-2x = 4$
- **$x = -2$**

11. Not-So-Simple Exponents: $9^{n+10} + 3 = 81$

- $9^{n+10} = 81 - 3$
- $9^{n+10} = 78$
- $n + 10 = \log_9 78$
- $n + 10 = \frac{\log 78}{\log 9}$; $\log 9 \rightarrow \log 3^2 \rightarrow 2 \log 3$
- $n + 10 = \frac{\log 78}{2 \log 3}$
- $n = \frac{\log 78}{2 \log 3} - 10$
- **$n = -8.0172$**

12. Quadratic Equations: $4b^2 + 8b + 7 = 4$; Round answer to 2 decimal places.

- $4b^2 + 8b + 7 - 4 = 0$
- $4b^2 + 8b + 3 = 0$
- $b = \frac{-(8) \pm \sqrt{(8)^2 - 4(4)(3)}}{2(4)}$
- $b = \frac{-(8) \pm \sqrt{64 - 48}}{8}$
- $b = \frac{-(8) \pm \sqrt{16}}{8}$
- $b = \frac{-(8) \pm 4}{8}$
- $b = \frac{-(8)-4}{8}$ AND $b = \frac{-(8)+4}{8}$
- $b = \frac{-12}{8}$ AND $b = \frac{4}{8}$
- **$b = \frac{-3}{2}$ AND $b = \frac{1}{2}$**

13. Trigonometry: $4\sin^2 x + 5 = 6$; $0 \leq x \leq 360$

- $4\sin^2 x = 1$
- $\sin^2 x = \frac{1}{4}$
- $\sin(x) = \frac{1}{2}, -\frac{1}{2}$
- **$x = 30^\circ, 150^\circ, 210^\circ, 330^\circ$**

14. Composite Functions: $f(x) = |x - 6| + x^2 - 1$ and $g(x) = 2x$; find $f(g(3))$

- $g(3) = 2(3)$
- $g(3) = 6$
- $f(6) = |6 - 6| + 6^2 - 1$
- $f(6) = 36 - 1$
- **$f(6) = 35$**